Vol. 9. No. 1. 2019

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www.crdeepjournal.org

International Journal of Basic and Applied Sciences (ISSN: 2277-1921)



<u>Full Length Research Paper</u> Bayesian Multilevel Model on determinants of off-Farm Income Diversification in Assosa Woreda, Benishangul Gumuz, Ethiopia

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| ARTICLE INFORMATION | ABSTRACT |
|--------------------------|---|
| Corresponding Author: | Introduction: Agriculture is the foundation of Ethiopia's economy, which contributes 45% GDP, more |
| O.Chandrasekhara Reddy | than 80% of employment opportunities and over 90% of the foreign exchange earnings of the country, but unable to cover the food requirement of the country due to shocks and trends. The non-farm |
| Article history: | enterprise sector plays a vital role in enhancing the wellbeing of rural households as it provide them |
| Received: 10-12-2019 | with income diversification opportunities. Objectives: The main objective of this research is to apply |
| Accepted: 18-12-2019 | Bayesian multilevel model in identifying determinants of off-farm income diversification from the non- |
| Revised: 25-12-2019 | farm sector in Assosa Woreda, Benishangul Gumuz region. Methods: Step-by-step modeling has been |
| Published: 30-12-2019 | used to analyze the data. Multilevel approach at both kebele and household level were considered. In Bayesian paradigm, the empty model, intercept model and intercept and slop model were employed. |
| Key words: | The convergence has been addressed using trace plot and autocorrelation. Results: The study indicated |
| Off-farming, Multilevel, | that Bayesian intercept model was found to be the best model. With this model, revealed that sex, |
| Bayesian | age, family size, education, Level of current income, access to credit, food security, proximity to town and scarcity of food and income are found to be significant, indicating strong effects on off-farm income engagement. The results indicated that the variability in the off-farming in the household level |
| | was greater than that of kebele level. Conclusion: The intercept model is selected to be the best model |
| | among the under used model. In considering the multilevel cluster the variability of off-farming in |
| | household level is more diversified than that of kebele level. The convergence assumption has been |
| | tested by using trace plot and autocorrelation method. |

Introduction

Agriculture is the foundation of Ethiopia's economy, which contributes 45% GDP, more than 80% of employment opportunities and over 90% of the foreign exchange earnings of the country, but unable to cover the food requirement of the country due to shocks and trends. Shocks are external events, such as erratic rain fall, flood, pests, disease, and market price fluctuation that adversely affect people's livelihood activities and trends are biophysical resources, demographic variables, and technical changes in production practices, economic condition, and educational status of households in a given area over time [1].

In recent years, the contribution of rural non-farm activities to household income diversification in developing world in general and sub-Saharan Africa in particular is increasing and contributes 30 to 45 percent of their income [2]. The non-farm enterprise sector plays a vital role in enhancing the wellbeing of rural households as it provide them with income diversification opportunities that helps in slowing down rural-urban migration, reducing poverty, and improving food security status [3]. [4]Argues that non-farm diversification is often a strategy that farm households use to moderate seasonal income variability and minimize the inherent risks associated with agriculture as a result of hostile agro-ecological factors.

Benishangul Gumuz Regional State (BGRS) is one of the poorest and most food insecure regions in the country. This is particularly, due to marginalization and isolation from development processes and initiatives [5]. In the region, agriculture accounts for about 93.2% of the people's livelihood, but its reward is poor due to labor-intensive rudimentary farming

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tools (shifting hoe cultivation practiced by indigenous people), high prevalence of crop pests, human disease and weeds (especially termite, malaria and striga respectively), erratic nature of rain fall, forest fire, poor infrastructure setting and extension services [6]. Despite increasing evidences on the potential contribution of non-farm income to economic wellbeing of rural households in the region, factors influencing their decision to diversify the activities are considerably overlooked. Therefore this study will investigate the determinants of nonfarm income diversification in Assosa woreda; Benishangul Gumuz Regional State.

Benishangul Gumuz Region is remained one of the least developed regions in the country Ethiopia and majority of its people in the areas face the challenges of critical food shortages and less income diversification. There are many Factors contributing to this problem. All these interwoven activities and situations deteriorating various potentials and opportunities expressed above and poverty is still widespread and continuously increasing in the region. Therefore, this research will attempt to identify sample household's major non-farm diversified income generating activities and systematically examine the determining factors for its income diversification which was not specifically touched by other researchers in this research area.

To the extent of researcher knowledge, most studies upon offfarm income diversification have been done routinely based on the frequentist approach. Incorporating Bayesian approach for estimation can give accurate result compared to frequentist approach [7]. Therefore, the major gap of this study is applying Bayesian approach to identify predictors of off-farm income diversification and its associated factors and to point out the cross-Kebele variation taking households' Kebele as random effects.

Research Questions

1. Are there any association between off-farm income

diversification and its covariate?

2. What are the factors that determine households' off--farm income diversification?

3. Does off-farm income diversification vary across households' Kebele?

The main objective of this research is to apply Bayesian multilevel model in identifying determinants of off-farm income diversification from the non- farm sector in Assosa Woreda, Benishangul Gumuz region.

The specific objectives of this research are to:

1. To investigate the association between off-farm income diversification and its covariate.

2. To examine factors determining households' off-farm income diversification.

3. To identify within and between households' Kebele variations.

Significance of the Study

Having clear picture and information on the livelihood strategies, food security status and their determinants in the study area can provide the basis for a detailed analysis on livelihood and food security in the country. A better understanding about non-farm income diversification behavior particularly in non agricultural sector will help in the design of policies that alleviates poverty, reduce vulnerability, and improve household well being. So, study will also provides direction for further research, extension, and development schemes that would benefit the farming population. Furthermore, the result may identify areas of intervention to alleviate poverty in general, food security in particular.

Materials and Methods

Description of the Study Area

Benishangul-Gumuz Regional State (BGRS): is one of the nine regional states established in 1995 by the new constitution of Ethiopia that created a federal system of governance. It is also recognized as one of the four 'emerging' or less developed regions in Ethiopia. Previously the southern part of BGRS belonged to Wollega while the area above the Abay River was under Gojjam province. The study woreda (Assosa): is one of the 21 woredas found in eastern parts of the Region, bordered by Kurmuk and Homesha in the north, Menge in the northeast, Oda Buldigilu in the east, Bambasi in the southeast, Mao-Komo special woreda in the south and by Sudan in the west. The 2007 national census reported that the total population of Assosa woreda is 87,366 of whom 23.25 percent was urban dwellers.

Sampling Procedures and Sample Size

A multi-stage sampling procedure will be employed in order to select sample households. In the first stage, out of the eight woredas (Assosa, Bambasi, Homosha, Kurmuk, Menge, Odabildagul and Sherkole) in Assosa Zone, Assosa woreda were the target of this research since its high population, accounts both settlers and indigenous people and residential areas of the researcher. In Assosa woreda there are 73 rural kebelles among which 35 of them are indigenous. And hence due to the existence of indigenous and settlers differing in culture and livelihood systems in the woreda, cluster sampling were used to identify woredas, where settler and indigenous people live.

In the second stage systematic random sampling were used to select sample population from each cluster. Systematic random sampling is the selection of every K^{th} element from a sampling frame, where K, is the sampling interval and K = total woreda in each cluster divided by sample size or K = N/n.

So, for, Indigenous population, K = 35/8 = 4.3 (four samples will be selected systematically as shown above). These are: Afaism, AtsetseAdirinunu, DabusAtimbaro and Rubalageda. In the case of Settlers, K = 38/8 = 4.3 (5 sample kebelles (Amba_1, Amba_10, Komshega_27, Menge_37 and Silga_24 will be selected).

In the third stage the desired number of households those who respond the interview questionnaires and Focus Group Discussions/FGD/ will be selected using the formula of sample size determination provided by YamaneTaro''s (1967) a simplified formula for sample sizes $(n=N/1+N (e^2),$

Where; N is the total population n is sample size e is the error margin. thus, n=87366/(1+87366*(0.05)²) n=87366/219.415 n= 398

Study Variables

Dependent variable:

The dependent variable considered for this study isoff-farm income diversification which a dichotomous random variable. Therefore, for this study, households who engaged in off-farm income were coded as 1 whereas households who were not engaged in off-farm income were coded as 0.

Explanatory variables

Explanatory variables considered in the study were selected based on some previous studies and those that are expected to be factors/determinants of off-farm income diversification. As

Methods of data Analysis

There are different statistical analyses that researcher has used for data analysis. Under this study researcher used Bayesian multilevel logistic regression.

Bayesian Multilevel Analysis of Random Coefficient Model

Since the logistic regression mode can be changed to linear using the logit link function, similarly in the multilevel analogue, random coefficient logistic regression is based on linear models for the logit link function that include random effects for the groups or other higher level units. Consider explanatory variables which are potential explanations for the observed outcomes. We can denote these variables by X_1, X_2, \dots, X_k . The values of X_h (h=1,2,3,...,k) are can also be assigned in the usual way by X_{hij} , since some or all of these variables could be level one(households) variables, the success probability is not necessarily the same for all individuals in a given group(region). Therefore, the success probability depends on the individual as well as the group, and is denoted by π_{ij} . Now consider a model with group specific regression of logit of the success probability *logit* (π_{ij}), on single level one explanatory variable X.

The expression $\sum_{h=1}^{K} U_{hj} X_{hij}$ can be considered as a random interaction between group and the explanatory variables. This model implies that the groups are characterized by two random effects: their intercepts and their slopes. It assumes that, for different groups the pairs of random effects $(U_{0j}, U_{hj}) = 1, 2, ..., k, j=1, 2, ..., 11)$ are independent and identically distributed. The random intercept variance, $var(U_{0j}) = \delta_0^2$, the random slope variance, $var(U_{1j}) = \delta_1^2$ and the covariance between the random effects, $cov(U_{0j}, U_{1j}) = \delta_{01}$ are called variance components [8].

Likelihood Function

The likelihood function used in Bayesian approach is equivalent to that of the classical inference. The joint distribution of n independent Bernoulli trials is the product of each Bernoulli

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suggested in the literature review, several variables that are associated with off-farm income diversification were considered as predictor variables. Therefore, those variables that are reviewed in the literature are listed below.

- Sex of house hold
- ✤ Age of house hold
- Education level of house hold
- Family size of house hold
- ✤ Marital Status
- Level of current income
- Food security of house hold
- Proximity to the nearest city
- Access to credit
- Feeding frequency of house hold above 15 years
- Feeding frequency of child
- Scarcity of food and income

Densities, where the sum of independent and identically distributed Bernoulli trials has a Binomial distribution. Specifically, let $Y_{1j}, Y_{2j}, \dots Y_{ij}$ be independent Bernoulli trials with success probabilities $\pi_{1j}, \pi_{2j}, \dots, \pi_{ij}$ that is $Y_{ij} = 1$ (women contraceptive use) with probability π_{ij} and $Y_{ij} = 0$ (not practicing off-farm income) with failure probability $1 - \pi_{ij}$, for i = 1, 2, ..., n and j = 1, 2, ..., 11. Since, the trials are independent, the joint distribution of $Y_{1j}, Y_{2j}, \dots, Y_{ij}$ is the product of n Bernoulli probabilities. The probability of success in logistic regression varies from one subject to another, depending on their covariates. Thus, the likelihood function is illustrated below as:

Where, π_{ij} represents the probability of the event for subject ij who has covariate vector X_{ij} , $y_{ij} = 1$ indicates the presence (offfarm income) and $Y_{ij}=0$ the absence (not engaged off-farm income) of the event for the given subject. The probability of success in logistic regression can be defined as:

$$\pi_{ij} = \frac{exp(p_O + U_{Oj} + \Sigma_{k=1}^K p_k x_{hij} + \Sigma_{k=1}^K U_{hj} x_{hij})}{1 + exp(\beta_O + U_{Oj} + \Sigma_{k=1}^K p_k x_{hij} + \Sigma_{k=1}^K U_{hj} x_{hij})}$$

Prior Distribution for random coefficient model

The prior distribution for the parameters for $\beta_0 \beta_1 \dots \beta_k$ and Ω_{μ} has been denoted as follow:

$$f(\beta j \mid data) = \prod_{i=1}^{n} \frac{1}{\sqrt{2\pi\sigma_{j}^{2}}} \exp\left\{\frac{-1}{2}\left(\frac{\beta_{j}-\mu_{j}}{\sigma_{j}}\right)^{2}\right\}$$

 $P(\Omega_u)$ a inverse – wishart (S_u^{-1}, v) denotes the inverse Wishart distribution with scale matrix S_u and degrees of freedom v. The parameter Ω_u is the variance covariance matrices. Equivalently, information about a variance-covariance matrix is represented by means of a Wishart (S_u, v) distribution placed on the precision matrix $\Omega_u^{-1}[9]$.

$P(\Omega_u^{-1}) \propto wishart(S_u, v)$

The Wishart distribution is the multivariate extension of the gamma distribution, although most statisticians use the Wishart distribution in the special case of integer degrees of freedom, in which case it simplifies to a multivariate generalization of the χ^2 distribution.

Posterior Distribution for random coefficient model .The posterior distribution is obtained as the product of the prior distribution of the parameters and the likelihood function. Therefore, using the above prior and likelihood function the full conditional posterior distribution for the parameters $\beta_0, \beta_1, \beta_2, \dots, \beta_K$ is given by:

$$f(\beta j \mid data) = \prod_{i=1}^{n} \left[\left(\frac{e^{\beta_0 + \beta_i X_{i1} + \beta_2 X_{i2} + \dots + \beta_p X_{ip}}}{1 + e^{\beta_0 + \beta_i X_{i1} + \beta_2 X_{i2} + \dots + \beta_p X_{ip}}} \right)^{y_i} \left(1 - \frac{e^{\beta_0 + \beta_i X_{i1} + \beta_2 X_{i2} + \dots + \beta_p X_{ip}}}{1 + e^{\beta_0 + \beta_i X_{i1} + \beta_2 X_{i2} + \dots + \beta_p X_{ip}}} \right)^{1-y_i} \right] - \\ \times \prod_{i=1}^{n} \frac{1}{\sqrt{2\pi\sigma_j^2}} \exp\left\{ -\frac{1}{2} \left(\frac{\beta_j - \mu_j}{\sigma_j} \right)^2 \right\}$$

[4]

Where h=1, 2, ..., K

And the full conditional distribution of the variance-covariance parameter Ω_{u} has been given as:

 $\begin{array}{ll} P(\Omega_u/\beta_\hbar U_{oj}, & Y_{ij})) & \propto & P(Y_{ij}/\beta_\hbar, \\ \Omega_u U_{oj},) P(U_{oj}/\Omega_u) P(\Omega_u) & [14] \end{array}$

Result and discussion

Descriptive statistics

This study was carried out to identify off-farm income diversification in Assosa woreda through analyzing the demographic and economic factors which were considered in similar studies conducted previously. In this study both descriptive and inferential analyses have been investigated for the purpose of identifying factor off-farm income diversification and food security nexus. Accordingly, the study used 398 households and the results are presented in two main parts. The first part of the result is the frequency distributions of all independent variables with their respective categories. The second part of the result is the chi-square test analysis (cross tabulation), with which the association between each explanatory variables and dependent variable (off-farm income). Consequently, the result obtained from descriptive analysis has shown number of households that are engaged in off-farm income. Therefore, the result indicated that out of 398 households considered in the analysis, 177(44.5%) households are engaged in off-farm income generating.

Test of heterogeneity proportions of off-farm income diversification

The two-level structure is used with the kebele as the secondlevel unit and the households' off-farm income as level one unit. This is based on the idea that there may be differences in households'off-farm income diversification between kebele that are not captured by the explanatory variables and hence may be regarded as unexplained variability within the set of all kebele [8]. Before attempting to multilevel analysis, one has to test the heterogeneity of households' off-farm income diversification among kebele of assosa woreda from which essential clues would be obtained for incorporating the random effects. Therefore, the Pearson chi-square for the proportion of households' off-farm income diversification across the kebele has been investigated in the table below. Consequently, as it can be observed in the Table 1, the Pearson Chi-square $(\chi^2 cal) = 53.672$ which is greater than 15.507 at 8 degree of freedom with P-value =7.99e-09 which is less than 0.05 level of significance, implying strong evidence of heterogeneity for offfarm income across kebele.

Test of Association

As mentioned earlier in methodology part in order to determine the association between off-farm income engagement and individual explanatory variables. Consequently, the result obtained in the Table 2 below clearly indicated that most of explanatory variables such as sex, age, education, marital status, Level of current income, feeding frequency households, Food security, Access to credit, Family size and Proximity to the town have significant association with at 5% level of significant. However, Feeding frequency of child, scarcity of food and income were statistically found to be non-significant at 5% level of significant.

Table .1 Chi-Square Tests of Heterogeneity of off-farm income between kebele.

| eterogeneitj er en rann mee | | |
|-----------------------------|---------|------------|
| Chi-square test | | |
| Statistics | Value | D.fP-value |
| Pearson Chi-square | 53.6728 | 7.99e-09 |
| N of valid cases | 398 | |

| Variable name | Degree freedom | Pearson's Chi-squared | p-value |
|--------------------------|----------------|-----------------------|----------|
| sex | 1 | 20.722 | 0.0132 |
| age | 2 | 33.894 | 0.0015 |
| education | 1 | 47.408 | 0.000035 |
| Marital status | 2 | 7.1999 | 0.02733 |
| Family size | 15 | 14.227 | 0.05084 |
| Level of current income | 3 | 22.006 | 0.044 |
| Feed_frequency_child | 2 | 4.6031 | 0.1001 |
| Feed_frequency_household | 2 | 8.3292 | 0.01554 |
| above 15 years | | | |
| Access to credit | 1 | 0.37797 | 0.0387 |
| Food security | 1 | 45.489 | 0.000026 |
| Scarcity_food_and_income | 1 | 0.67648, | 0.4108 |
| Proximity to the town | 1 | 29.661 | 0.00172 |

Source: own computation.

Bayesian multilevel logistic regression model comparisons Here the comparisons of Bayesian multilevel models such as multilevel empty model, random intercept model, and random coefficient model were conducted based on Deviance information criterion which is mostly used as model comparison in Bayesian analysis. Therefore, as it is shown in the Table 3 below the Bayesian random intercept model is appropriately fitting the off-farm income among kebeles of household data sets as compared to empty and random slope model.

| Table 3. | . Bayesian | multilevel | model | comparisons |
|----------|------------|------------|-------|-------------|
|----------|------------|------------|-------|-------------|

| Model comparison statistics | Empty model | Random intercept model | Random coefficient model |
|-----------------------------|-------------|------------------------|--------------------------|
| DIC | 423.4853 | 241.0768 | 349.8605 |

Bayesian intercept model

The results of the Bayesian intercept model in table 4.3 revealed that sex, age, family size, education, Level of current income, access to credit, food security, proximity to town and scarcity of food and income are found to be significant, indicating strong effects on off-farm income engagement because their corresponding p-value is less 5% level significant(α). It is also observed that the odds of engaged off-farm income for young households are $27.32(OR = e^{3.3078})$ times more than old households engaged in off-farm income. The odds of engaged in off-farm income for female household is 0.93 ($OR = e^{-2.7271}$) less than male households. Similarly, the odds of engaged in offfarm income for literate households are 7.04 ($OR = e^{1.9511}$) times more than illiterate households. The odds of engaged in off-farm income for households whose level of current income high is $0.80(OR = e^{-1.5954})$ less than those whose level of current income is very high. And also the odds of engaged in offfarm income for households whose level of current income medium is 0.9 ($OR = e^{-2.2633}$) less than those those level of

current income is very high. Furthermore, the odds of engaged in off-farm income for households whose level of current income low $0.9(OR = e^{-2.3078})$ less than those whose level of current income is very high. The odds of engaged in off-farm income for households is 0.0321 when average income of households increased by one unit.

The odds of engaged in off-farm income for households who can't get access to credit 0.79 ($OR = e^{-1.5421}$)less than households who can get access to credit. The odds of engaged in off-farm income for households who have food security are $3652.6(OR = e^{9.2032})$ times more than those who have no food security. The odds of engaged in off-farm income for households who live far from town is $0.69(OR = e^{-2.1398})$ less than households who live near to town. Moreover, the odds of engaged in off-farm income is $0.999(OR = e^{-7.0870})$ less than households who have no scarcity of food and income.

| Variable name | Fixed effect | | | | | | |
|----------------------------|---------------------|------------|--------|----------|---------|---------|---------|
| | Categories | post. mean | SD | Sd.error | 2.5% | 50% | 97.5% |
| intercept | βο | 0.2506 | 1.9446 | 0.0869 | 4.0022 | -0.2333 | 3.4892 |
| Sex | female | -2.7271 | 0.5403 | 0.0242 | -3.7441 | -2.7058 | -1.599 |
| | Ref(male) | | | | | | |
| Age | Young | 3.3078 | 1.0167 | 0.0455 | 1.2676 | 3.2844 | 5.5523 |
| C | Adult | 3.4413 | 1.0206 | 0.0456 | 1.5841 | 3.3871 | 5.6562 |
| | Ref(old) | | | | | | |
| Education | Literate | 1.9511 | 0.5107 | 0.0228 | 0.9535 | 1.9372 | 2.9680 |
| | Ref (illiterate) | | | | | | |
| Marital status | Single | 0.9122 | 1.0594 | 0.0474 | -1.1965 | 0.8878 | 3.0758 |
| | Divorced | 0.6001 | 0.8973 | 0.0401 | -1.0871 | 0.6095 | 2.2545 |
| | Ref (married) | | | | | | |
| Family size | size | 0.2418 | 0.0869 | 0.0039 | 0.4142 | 0.2403 | 0.0825 |
| Level of income | High | -1.5954 | 0.7985 | 0.0357 | -3.1919 | -1.5369 | -0.0361 |
| | Medium | -2.2633 | 0.7016 | 0.0314 | -3.7410 | -2.2410 | -0.9837 |
| | Low | -2.3047 | 0.6963 | 0.0311 | -3.7673 | -2.2852 | -1.1036 |
| | Ref(very high) | | | | | | |
| Feeding frequency HH | 3 times | -0.2923 | 0.4909 | 0.0230 | -1.2216 | -0.2958 | 0.6957 |
| | > 3 times | 1.1860 | 2.3298 | 0.1042 | -3.1044 | 1.0618 | 6.1970 |
| | Ref(twice and less) | | | | | | |
| Feeding frequency of child | 3 times | 2.3725 | 1.4331 | 0.0641 | -0.3597 | 2.2994 | 5.1914 |
| | >3 times | 2.0086 | 1.5373 | 0.0688 | -0.9205 | 2.0142 | 4.8948 |
| | Ref(twice and less) | | | | | | |
| Food security | Yes Ref(No) | 8.2032 | 1.3073 | 0.0585 | 6.2655 | 7.9159 | 11.4788 |

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|-------------------|-------------------------------------|---------------|----------------|------------|-----------|---------------|---------|
| Proximity to town | far | -2.1398 | 0.5094 | 0.0228 | -3.0301 | -2.1707 | -0.9845 |
| | Ref(near) | | | | | | |
| Scarcity food and | No | -7.0870 | 1.0919 | 0.0488 | -9.3797 | -6.9628 | -5.2836 |
| income | | | | | | | |
| | Ref(Yes) | | | | | | |
| Access to credit | No | -1.5421 | 0.6317 | 0.0282 | -2.7199 | -1.5778 | -0.3244 |
| | Ref(Yes) | | | | | | |
| Random effect | | | | | | | |
| Kebele | $\operatorname{var}(\Box_{\Box}^2)$ | | 2.289 | | | 1.981 0.08859 | 0.4957 |
| | <-U/ | | | | 1.1 | 124 7.503 | |

Intra class correlation

Under this situation, researcher can usually interpret the variation of intercept $\square_{\square\square\square\square\square}^2$ between cluster(in this case Kebele) by considering the ICC which goes from 0 indicates perfect independence of residuals or the observations do not depend on cluster membership and 1 indicates perfect interdependence of residuals or the observations only vary between clusters[10]. It is usually expressed as :-

$$\Box \Box \Box = \frac{\Box_{000000}^{2}}{\Box_{000000}^{2} + \Box_{0}^{2}}$$

Where $\Box_{\square\square\square\square\square}^2$ is the variance of the between cluster and \Box_{\square}^2 the variance of the residual. But, in the context of logistic regression, there is no direct estimation or calculation of the residuals on the first level. Therefore, \Box_{\square}^2 is the logistic distribution variance which always can be given the value Ξ_3^2 is 3.29. The intra kebele correlation coefficient for this study was estimated $\widehat{\Box} = \frac{2.289}{2.289+3.29} = 0.41$. This indicated that about 41% of the total variability in off-farm income diversification due to the fact that differences across Kebele and the remaining unexplained 59% accounts the between households differences.

Checking Convergence

Checking the convergence of an MCMC algorithm would be a pre-condition issue for the exact estimation of the posterior distribution of interest. For this reason, both the length of the burn in period and the size of the MCMC output that was used for the posterior analysis could be specified by the user. The other most important problem for checking convergence is specification of the thinning interval, that is, the numbers of iterations researcher needs to discard until two successive observations become independent. Regarding this, Metropolis-Hasting algorithm methods was implemented for this study with 60000 iterations, 10000 burn-in terms discarded, and 50 thinning interval to make observations independent or low autocorrelation. Therefore, two different methods such as trace plot and density plot for monitoring convergence have been presented below.

Trace plots: This is the graph which would be plotted the number of iterations versus the generated values. In this graph convergence can be attained if all values are within a zone without strong periodicities (up and down periods). Therefore, the trace plots are all straight line which did not show up and down periods.

Density plot: the density plots are almost similar with normal plot. This is an indication that all posterior estimates were

converged. The trace and density plots can be found in appendices (see appendix A).

Conclusion

This study was aimed to apply Bayesian multilevel model in identifying determinants of off-farm income diversification from the non- farm sector in Assosa Woreda, Benishangul Gumuz region.

In order to address the basic research questions, the researcher considered different statistical methods to select the appropriate sample size and corresponding model.

Three different models were considered and the Bayesian intercept model was found to be the best model. With this model, revealed that sex, age, family size, education, Level of current income, access to credit, food security, proximity to town and scarcity of food and income are found to be significant, indicating strong effects on off-farm income engagement. In identifying the within and between cluster correlation, the intra correlation methods was applied and indicted that the variability in the off-farming in the household level was greater than that of kebele level. The study also checked the convergence; especially the convergence in the random effects has been checked and fitted very well using trace plot and autocorrelation.

Competing interests

The authors declare that they have no competing interest

Funding

All the expenses for the accessing of the data and related were covered the expenses from the authors

Authors' contributions

This study was designed and compiled by EM as the principal investigator. The development of the basic research questions, identifying the problems and selecting appropriate statistical models have been done collaboratively by EM and EA. Edition of the overall progress of the work MD

Acknowledgements

We thank Benishangul Gumuz Agricultural office for supporting us all the necessary data and relevant materials.

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Trace of V2adult

30000

Iterations

Trace of V2young

30000

10000

50000

50000

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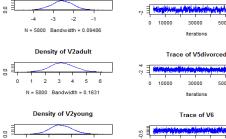
8

50000

Trace of (Intercept) Density of (Intercept) Trace of V4literate g I 30000 50000 30000 10000 Iteration N = 5800 Bandwidth = 0.383 Iterations Density of V1female Trace of V1female Trace of V5single 8 1 30000 50000 -3 -2 30000 10000 Iterations N = 5800 Bandwidth = 0.09486 Iterations

8

Fig A: Trace and density plot



N = 5800 Bandwidth = 0.1757

10000

30000

N = 5800 Bandwidth = 0.2143 Density of V5divorced 8 N = 5800 Bandwidth = 0.1634 Density of V6

Density of V4literate

N = 5800 Bandwidth = 0.0981

Density of V5single

-0.6 -0.4 -0.2 0.0 N = 5800 Bandwidth = 0.01685

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